

# PROBLEM SOLVING PARADIGM



Riddles / Puzzles / Paradoxes / Anomalies / Fallacies / Inconsistencies / Counter-Intuitive Behavior / etc.

### PROBLEM SOLVING PARADIGM

**Complexity** Human necessity to deal-with (simplify) the complexity in the problem-space

Simplification of Science -&- Science of Simplification

**Combinatorial Complexity** 

**Organized-Complexity** 

(Systems Approach)

Unorganized-Complexity

What How (WHY) Where When Which / Who ...

## **A Problem Solving Scenario**

Trial & Error (hit or miss) - as a default approach

• • •

An iterative approach incorporating a sequence of some well defined steps/stages with the option at every step/stage for a possible iteration of any earlier subsequence

• •

**Detection / Description** 

**Identification / Classification** 

**Representation / Formulation / Modeling** 

Solution: Analysis / Simulation / Synthesis / Design / Optimization / Control

**Testing / Interpretation / Evaluation** 

**Implementation** 

### **SOME ISSUES OF CONCERN**

Missing the relevant detail (Signal) -and/or- Picking the irrelevant detail (Noise)

**Observer – Observation – Observed** : Scope, Resolution/Granularity

**Modeling Errors - Implicit / Hidden Assumptions** 

Errors of Decomposition -&- Errors of Composition

**Complementarity** - Interdependence, Self-Reference / Circularity / non-Transitivity

Performance: Robustness, Reliability, Efficiency, Safety, . . .

Dynamics: Regulation, Adaptation, Control, Stability, Equilibrium, Convergence

**Optimization** 

Uncertainty

. . .



#### **EXAMPLE:**

A: rated 3-out-of-6 with 100% weightage.

B: rated 2-out-of-6 with 55% weightage, 4-out-of-6 with 25% weightage, 6-out-of-6 with 20% weightage.

C: rated 1-out-of-6 with 52% weightage, 5-out-of-6 with 48% weightage.

[Higher rating indicates better preference]

Determine the rank-order-of-preference for deciding on the best, second-best and the third.

#### **Three Approaches:**

Compare the weighted average ratings for each of the candidate-choices A,B,C (evaluated one at a time);

{A=3.00; B=3.30; C=2.92}

Result: B>A>C.

Compare two at a time: (i)  $P\{A > B\} = 0.55$ ; (ii)  $P\{B > C\} = 0.616$ ; (iii)  $P\{A > C\} = 0.52$ ;

Result: A>B>C.

Compare three at a time: (i)  $P\{(A>B)&(A>C)\}=0.286$ ; (ii)  $P\{(B>A)&(B>C)\}=0.330$ ; (iii)  $P\{(C>A)&(C>B)\}=0.384$ ;

Result: C>B>A.

## Simpson's Reversal Paradox -OR- Discrimination Statistics

[Yule-Simpson Effect]

	M	F		M	F		M	F	
S	11	70		80	19		91	89	S
R	9	30	+	20	1	<b>=</b>	29	31	R
	M	F		M	F		M	F	
S	1	5		20	9		21	14	S
R	19	45	+	30	11		49	<b>56</b>	R
	M	F		M	F		M	F	
S	1	5		45	19		46	24	S
R	19	45	+	5	1		24	46	R
	M	F		M	F		M	F	

	M	F		M	F		M	F	
S	10	30		70	40		80	70	S
R	30	<b>70</b>		30	10		<b>70</b>	80	R
	M	F		M	F		M	F	
S	50	25		15	30		65	55	S
R	50	25	<b>+</b>	35	<b>70</b>	_	85	95	R
	M	F		M	F		M	F	
S	6	11		9	4		15	15	S
R	4	9	+	11	6		15	15	R
	S	F		M	F		M	F	

## **Non-Transitivity** => Cycle / Circularity

Team-A: scores 100 always.

Team-B: scores 101 three-fourth-of-the-time and 97 one-fourth-of-the-time.

Team-C: scores 102 half-of-the-time and 98 half-of-the-time.

Team-D: scores 103 one-fourth-of-the-time and 99 three-fourth-of-the-time.

[Higher score indicates better performance]

#### Weighted-time-average-scores:

```
wtas-A = wtas-B = wtas-C = wtas-D = 100.

P{A<B} = 0.7500; P{B<A} = 0.2500;

P{A<C} = 0.5000; P{C<A} = 0.5000;

P{A<D} = 0.2500; P{D<A} = 0.7500;

P{B<C} = 0.3750; P{C<B} = 0.6250;

P{B<D} = 0.5625; P{D<B} = 0.4375;

P{C<D} = 0.3750; P{D<C} = 0.6250;
```

**Observe the cycles arising from non-transitivity:** 

```
(A<B<D<A);
```

(D < C < B < D);

### **Self-reference / Circularity**

[Liar Paradox]

- (1) "This sentence is *False*"
- (2) "This sentence is not *True*"
- (3) "This sentence is *Only False*"
- (4) "This sentence contains seven words"
- (5) "This sentence does not contain seven words"
- (6) A: "Sentence-B is *True*"; B: "Sentence-A is *False*"
- (7) S1: "Sentence S2 is False"; S2: "Sentence S3 is False"; S3: "Sentence S1 is False"

## **Self-reference** / **Circularity**

#### ESCHER DRAWING HANDS DREW HANDS DRAWING ESCHER



ESCHER DRAWING HANDS DREW HANDS DRAWING ESCHER

### **SYMMETRY**

Effect of G:R:A:N:U:L:A:R:I:T:Y on Symmetry Properties

**Palindrome-String:** String-Sf = String-Sr

<b>S</b> ↓ <b>p</b> →	р1	<b>p2</b>	р3	p4	р5	p6	р7	p8	р9
Sf:	Q1	Q2	Q3	Q4	Q5	Q6	Q7	Q8	Q9
Sr:	Q9	Q8	Q7	Q6	Q5	Q4	Q3	Q2	Q1

Sf:	M	A	L	A	Y	A	L	A	M
Sr:	M	A	L	A	Y	A	L	A	M

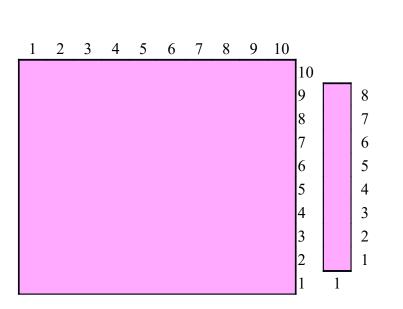
S↓ p→	<b>p1</b>	p2 p3		p4 p5		p6	р7
Sf:	Escher	drawing	hands	drew	hands	drawing	Escher
Sr:	Escher	drawing	hands	drew	hands	drawing	Escher

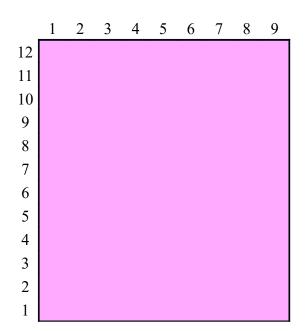
### **CARPET CUTTING & STITCHING PUZZLE**

Given: One piece of Carpet 10x10 size, and another piece of Carpet 1x8 size;

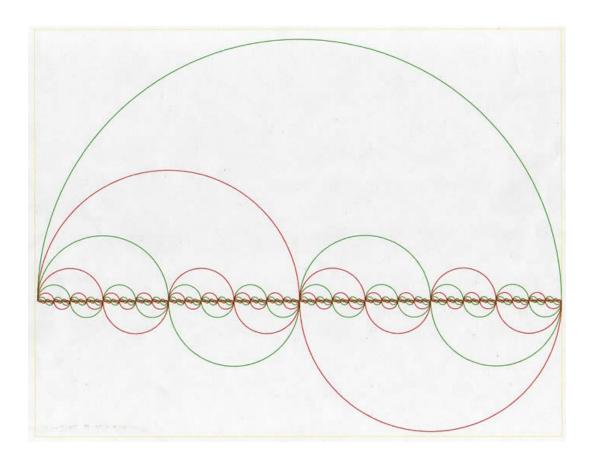
Goal: To make a single piece carpet 9x12 size;

Condition: Carpet 1x8 is not to be cut at all, whereas Carpet 10x10 can be cut into no more than two pieces, before joining.





## **Circumference - Diameter Paradox**

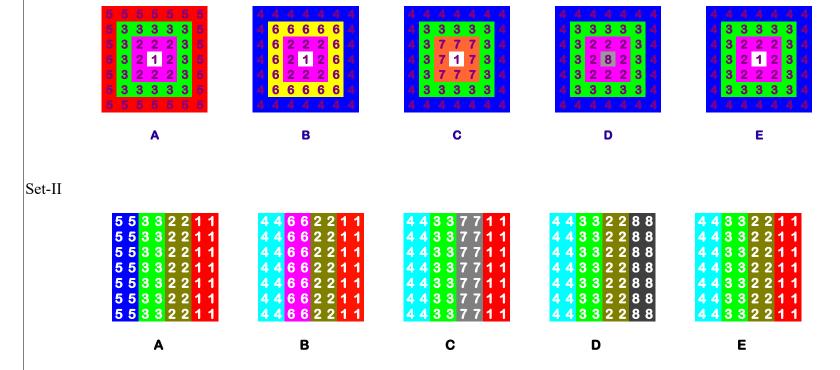


-----

#### ! THE MOST DIFFERENT from THE MOST SIMILAR!

Q: Identify the one figure that is (1) most different from (2) most similar to - the others, among the following set of five given figures (A), (B), (C), (D), (E) - [you may chose either Set-I or Set-II]. Explain / Justify your answers.

Set-I



There are only 10 types of people in the world  $\circ$   $\circ$   $\circ$   $\circ$   $\circ$   $\circ$   $\circ$   $\circ$  Those who understand binary and those who don't ... Mystery ... Amazement ... Wonder ... ... to be resolved ... ... keeping ... the wonderful ... undisturbed ...

THANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOU HANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUT ANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTH NKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHA KYOUTHANKYOUTHA YOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANK OUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKY UTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYO THANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOU HANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUT ANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTH NKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHA KYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHAN YOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANK OUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKY UTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYO THANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOU HANKYOUTHANKYOU ANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTH NKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHA KYOUTHANKYOUTHA YOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANK OUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKY UTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYOUTHANKYO